

Spiral Galaxies When Disks Dominate their Halos (using Arm Pitches and Rotation Curves)

S. Howard (USNO/retired) and G. Byrd (U. Alabama/emeritus)

GOAL Using observation and dynamical theory we show that some spiral galaxies are disk dominated rather than halo dominated over their density wave arm regions (even with flat rotation curves).

DISK SURFACE DENSITY

$$\mu_{D,V} = 2 \left(\frac{V^2}{\pi G} \right) \left(\frac{\tan i_m}{mr} \right) \left[1 + \frac{m(1-r/r_{CR})}{\sqrt{2}} \right]$$

PURE HALO MASS ILR to OLR.

$$M_{100\%,H} = \left(\frac{V^2}{G} \right) (r_{OLR} - r_{ILR})$$

MASS RATIO

Integrated disk surface density mass ILR to OLR = M_D .

F_D = Mass ratio of M_D actual disk to $M_{100\%,H}$ ILR to OLR.

$$F_D = 4 \tan i / m.$$

Actual Halo = $1 - F_D$
ILR to OLR

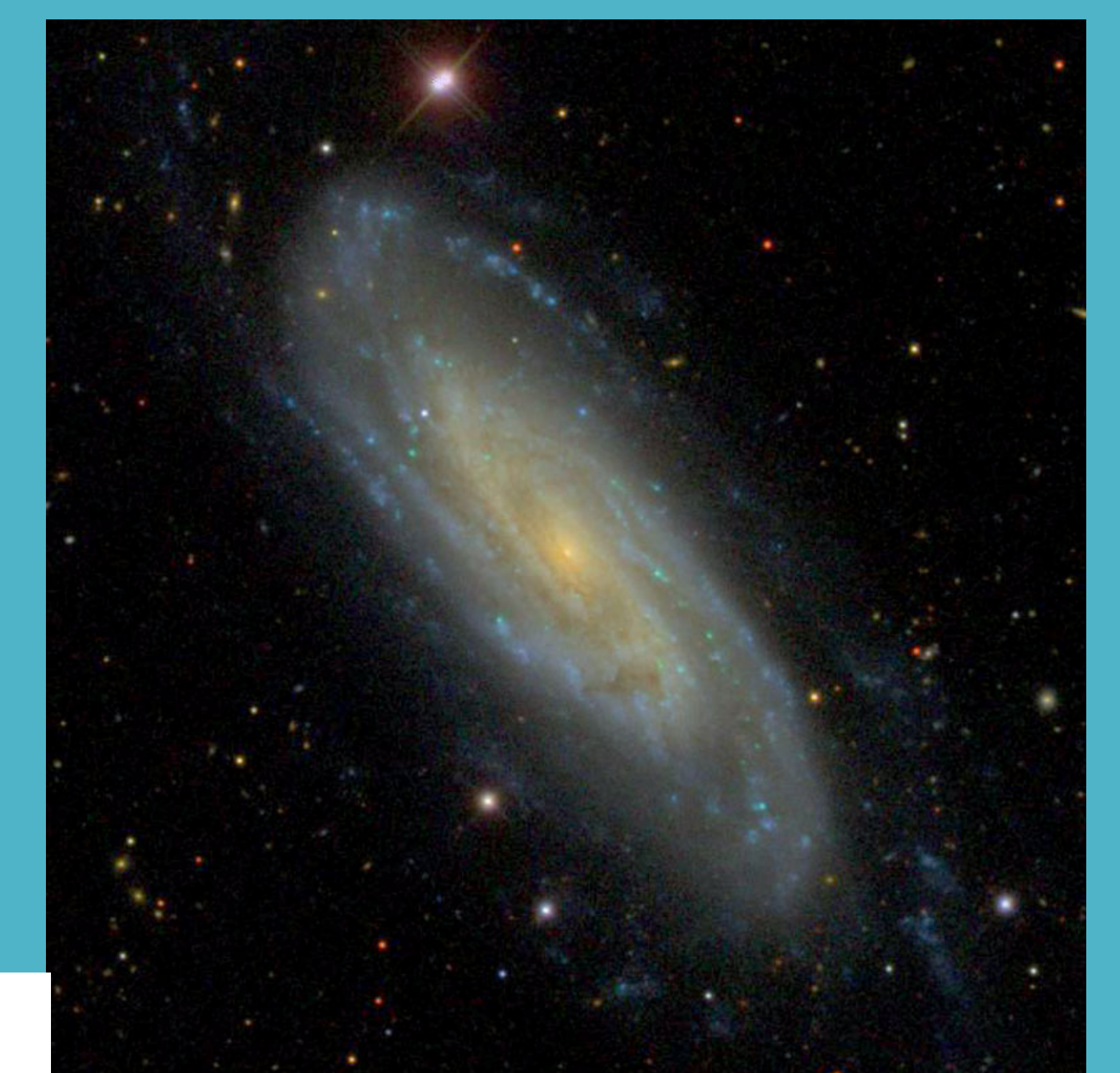
VARIABLES

μ_D	= disk surface mass density
$\Omega = V/r$	= flat V orbital angular rate
r_{CR}	= co-rotation radius
$\Omega_p = V/r_{CR,nn}$	= angular rate pattern speed
m	= multiplicity of arms
a	= velocity dispersion for arm stability
r_{ILR}	= inner Lindblad resonance radius
r_{OLR}	= outer Lindblad resonance radius

EXAMPLES



NGC 7217, Halo Dominated



NGC3198, Disk Dominated

i = pitch angle of spiral arm	r = radius ILR to OLR	Disk Dominance, F_D
NGC 7217, tightly wound ,	$i = 4.8^\circ$	0.13
M100,	$i = 18^\circ$	0.63
M51,	$i = 15^\circ$	0.54
M101,	$i = 20^\circ$	0.73
NGC 3198, loosely wound	$i = 30^\circ$	0.86

Increasing disk significance

For more details see link,

[\(4\) \(PDF\) Spiral Galaxies When Disks Dominate their Halos \(using Arm Pitches and Rotation Curves\) \(researchgate.net\)](#)